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SET B



**INDIAN SCHOOL MUSCAT
HALF YEARLY EXAMINATION
SUBJECT : MATHEMATICS**

CLASS: XII

Sub.Code:041

Time Allotted: 3 Hrs.

22.09.2019

Max.Marks: 80

General Instructions:

- (i) All questions are compulsory.
- (ii) This question paper contains 36 questions.
- (iii) Question 1- 20 in Section A are MCQ/Very short-answer type questions carrying 1 mark each.
- (iv) Question 21-26 in Section B are short-answer type questions carrying 2 marks each.
- (v) Question 27-32 in Section C are long-answer-I type questions carrying 4 marks each.
- (vi) Question 33-36 in Section D are long-answer-II type questions carrying 6 marks each.

	SECTION A	
1.	Find the area bounded by the curve $y = \cos x$, between $x = 0$ and $x = 2\pi$.	1
2.	Evaluate: $\int \log x \, dx$	1
3.	Find the value of $\tan^{-1}(1) + \cos^{-1}\left(-\frac{1}{2}\right) + \sin^{-1}\left(\frac{1}{2}\right)$	1
4.	If $f, g : \mathbb{R} \rightarrow \mathbb{R}$ be two functions defined as $f(x) = x + x$ and $g(x) = x - x$, for all x in \mathbb{R} , find $f \circ g(-5)$.	1
5.	Find the value of $\cos^{-1} \cos\left(\frac{5\pi}{4}\right)$.	1
6.	Evaluate: $\int_{-1}^1 [x] dx$	1
7.	Evaluate: $\int \frac{1 - \cos 2x}{1 + \cos 2x} dx$	1
8.	Evaluate : $\int_0^{2\pi} \sin x \, dx$	1
9.	Find the area bounded by the lines $y = x$ and $x = 3$ in the first quadrant.	1
10.	A point C in the domain of a function f at which either $f'(c) = 0$ or f is not differentiable is called -----.	1

11.	The line $y = x + 1$ is a tangent to the curve $y^2 = 4x$ at the point a) (1, 2) b) (2, 1) c) (1, -2) d) (-1, 2)	1
12.	$f(x) = \begin{cases} x \sin \frac{1}{x}, & x \neq 0 \\ k, & x = 0 \end{cases}$ is continuous at $x = 0$. Find k. a) 8 b) 1 c) -1 d) 0	1
13.	If $y = x + e^x$, then $\frac{d^2x}{dy^2} = \text{-----}$ a) $\frac{1}{(1+e^x)^2}$ b) $\frac{-e^x}{(1+e^x)^2}$ c) $\frac{-e^x}{(1+e^x)^3}$ d) e^x	1
14.	Let R be the relation in the set N given by $R = \{(a, b) : a = b - 2, b > 6\}$. Choose the correct answer. A) (2,4) \in R B) (3,8) \in R C) (6,8) \in R D) (8,7) \in R	1
15.	$f(x) = \begin{cases} ax^2 + 1, & x > 1 \\ x + a, & x \leq 1 \end{cases}$ is differentiable at $x = 1$, then find the value of a. a) 2 b) 1 c) 0 d) $\frac{1}{2}$	1
16.	The interval in which $y = x^2 e^{-x}$ is increasing is a) $(-\infty, \infty)$ b) $(-2, 0)$ c) $(2, \infty)$ d) $(0, 2)$	1
17.	Let $f : \mathbb{R} \rightarrow \mathbb{R}$ be defined as $f(x) = x^4$. Choose the correct answer. a) f is one- one onto b) f is many-one onto c) f is one-one but not onto d) f is neither one-one nor onto.	1
18.	Choose the correct principal value branch of the range of $y = \tan^{-1} x$. a) $\left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$ b) $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$ c) $[0, \pi]$ d) $(0, \pi)$	1
19.	Find the area bounded by $f(x) = x $, between $x = -3$ and $x = 3$. a) 0 b) 18 sq.units c) 9 sq.units d) 6 sq.units	1
20.	Find the derivative of $\sin(x)^3$ with respect to $\cos(x)^3$. a) $-\tan(x^3)$ b) $-\cot(x^3)$ c) $\cot(x^3)$ d) $\tan(x^3)$	1
SECTION B		
21.	Find $\int_1^4 f(x)dx$, if $f(x) = \begin{cases} 7x & ; \text{if } 1 \leq x \leq 3 \\ 8 & ; \text{if } 3 \leq x \leq 4 \end{cases}$ OR Evaluate: $\int \frac{5^{(7x-5)}}{5^{(2x+10)}} dx$	2
22.	Find the value of k, if the following function is continuous at 1 $f(x) = \begin{cases} k(x^2 - 2), & x \leq 1 \\ 4x + 1, & x > 1 \end{cases}$	2
23.	Find $\frac{dy}{dx}$ if, $y = \sin^{-1}\left(\frac{1-x^2}{1+x^2}\right)$ $0 < x < 1$	2
24.	Prove that $\tan^{-1}\left(\frac{1}{2}\right) + \tan^{-1}\left(\frac{2}{11}\right) = \tan^{-1}\left(\frac{3}{4}\right)$ OR Evaluate: $\sin\left(\frac{1}{2} \cos^{-1} \frac{4}{5}\right)$	2

25.	The total cost $c(x)$ associated with the production of x units of an item is given by $C(x) = 0.007x^3 - 0.003x^2 + 15x + 4000$. Find the marginal cost when 17 units are produced.	2
26.	Evaluate: $\int \sqrt{\frac{a+x}{a-x}} - \sqrt{\frac{a-x}{a+x}} dx$	2
	SECTION C	
27.	Find $\frac{dy}{dx}$, $y = (\cos x)^{\sin x} + x^{\log x}$	4
28.	$f: \mathbf{N} \rightarrow \mathbf{N}$ be defined by $f(x) = \begin{cases} x+1, & \text{if } x \text{ is odd} \\ x-1, & \text{if } x \text{ is even} \end{cases}$ for all $x \in \mathbf{N}$, show that f is bijective.	4
29.	Find the intervals in which the functions given below are strictly decreasing or strictly increasing:- $f(x) = \frac{3}{10}x^4 - \frac{4}{5}x^3 - 3x^2 + \frac{36}{5}x + 11$ OR Find the equations of the tangent and normal to the curve $y = \frac{x-7}{(x-2)(x-3)}$ at the point, where it cuts x -axis.	4
30.	Simplify: $\tan^{-1} \left[\frac{\sqrt{1+x} - \sqrt{1-x}}{\sqrt{1+x} + \sqrt{1-x}} \right]$	4
31.	If $f(x) = \begin{cases} x^2 + 3x + a, & x \leq 1 \\ bx + 2, & x > 1 \end{cases}$, is differentiable. Find a and b . OR If $f(x) = \begin{cases} \frac{1-\sin^3 x}{3\cos^2 x}, & x < \frac{\pi}{2} \\ a, & x = \frac{\pi}{2} \\ \frac{b(1-\sin x)}{(\pi-2x)^2}, & x > \frac{\pi}{2} \end{cases}$ is continuous at $x = \frac{\pi}{2}$, find a and b .	4
32.	Evaluate: $\int \frac{5x-2}{3x^2+2x+1} dx$	4

